

## Supplementary material to

### INTERNAL MODEL CONTROL OF CUMENE PROCESS USING ANALYTICAL RULES AND EVOLUTIONARY COMPUTATION

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The closed-loop setpoint response of the system shown in Figure1 can is represented as,

$$\frac{y}{y_s} = \frac{g(s)c(s)}{g(s)c(s)+1} \quad (\text{A1})$$

Here we have assumed that output measurement  $y$  is perfect. In the IMC PID controller, the desired closed-loop response will be specified first, and we will develop a controller that matches the desired closed-loop response.

$$c(s) = \frac{1}{g(s)} \frac{1}{\left(\frac{y}{y_s} - 1\right)} \quad (\text{A2})$$

We consider the first-order and second-order time delay model  $g(s)$  in Eqs. (9) and (11). For the first-order time delay model, the desired response can be equated to Eq. (9)

$$\left(\frac{y}{y_s}\right)_{desired} = \frac{e^{-\theta s}}{\tau_c s + 1} \quad (\text{A3})$$

We have kept the delay  $\theta$  in the “desired” response, which gives a “Smith predictor” controller and can be expressed as

$$c(s) = \frac{(\tau_1 s + 1)}{K} \frac{1}{(\tau_c s + 1 - e^{-\theta s})} \quad (\text{A4})$$

for FOPDT model

$\tau_c = \text{tuning parameter}$

$e^{-\theta s} = 1 - \theta s$ , First order Taylor series approximation is applied for the delay. The resultant response can be expressed as

$$c(s) = \frac{(\tau_1 s + 1)}{K} \frac{1}{(\tau_c + \theta)s} \quad (\text{A5})$$

$$c(s) = K_c \left(1 + \frac{1}{\tau_I s}\right) \quad (\text{A6})$$

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From the comparison of Eqs. (17) and (18), the parameters can be obtained as

$$\tau_I = \tau_1, K_c = \frac{1}{K} \frac{\tau_I}{(\tau_c + \theta)} \quad (\text{A7})$$

Similarly, the second-order response with a time constant  $\tau_c$  can be represented as

$$c(s) = \frac{(\tau_1 s + 1)(\tau_2 s + 1)}{K} \frac{1}{(\tau_c s + 1 - e^{-\theta s})} \quad (\text{A8})$$

After the first-order Taylor series approximation of the delay SOPDT model is represented as

$$c(s) = \frac{(\tau_1 s + 1)(\tau_2 s + 1)}{K} \frac{1}{(\tau_c + \theta)s} \quad (\text{A9})$$

$$c(s) = K_c \left( \tau_D s + \frac{1}{\tau_I s} + \left( \frac{\tau_D}{\tau_I} + 1 \right) \right) \quad (\text{A10})$$