

## Supplementary material to

### THERMODYNAMIC MODELING OF GAS SOLUBILITY IN IONIC LIQUIDS USING EQUATIONS OF STATE

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### SUPPLEMENTARY A - CH<sub>4</sub>, CO<sub>2</sub>, and H<sub>2</sub>S results

#### Supplementary A1. Parameters of the EoS

The section contains the parameters obtained for CH<sub>4</sub>, CO<sub>2</sub>, and H<sub>2</sub>S from the SRK, CPA, and PC-SAFT EoS, which were taken from the literature, as shown in the following tables.

Table S1. Pure component parameters from SRK EoS [1].

Components	MM [g/mol]	T <sub>c</sub> [K]	P <sub>c</sub> [bar]	ω [-]
CH <sub>4</sub>	16.04	190.56	45.99	0.0115478
CO <sub>2</sub>	44.01	304.21	73.83	0.2236210
H <sub>2</sub> S	34.08	373.30	89.63	0.0941677

Table S2. Pure component parameters from CPA EoS.

Components	MM [g/mol]	m <sub>m</sub> [-]	T <sub>cm</sub> [K]	P <sub>cm</sub> [bar]	$\frac{\epsilon^{AB}}{R}$ [K]	$\beta^{AB}$ [-]	Associative schemes	Reference**
CH <sub>4</sub>	16.04	0.4516	193.18	47.82			NA*	[2]
CO <sub>2</sub>	44.01	0.7728	309.93	82.08				
H <sub>2</sub> S	34.08	0.6389	313.35	77.97	454.87	0.2329	3B***	[3]

\*\*NA: Non-associative. \*\*The parameters b<sub>CPA</sub>, a<sub>0</sub>, c<sub>1</sub>, ε<sup>AB</sup> e β<sup>AB</sup> were obtained and the parameters m<sub>m</sub>, T<sub>cm</sub>, P<sub>cm</sub>, ε<sup>AB</sup>/R e β<sup>AB</sup> were calculated. \*\*\*3B: Associative type 3B.

Table S3. Pure component parameters from PC-SAFT EoS.

Components	MM [g/mol]	m [-]	σ [Å]	$\frac{\epsilon_{ij}}{k_b}$ [K]	$\frac{\epsilon^{AB}}{k_b}$ [K]	K <sup>AB</sup> [-]	Associative schemes	Reference
CH <sub>4</sub>	16.04	1.0000	3.7039	150.03			NA*	[4]
CO <sub>2</sub>	44.01	2.0729	2.7852	16.21				
H <sub>2</sub> S	34.08	1.6490	3.0550	229.84	536.6	0.001	2B**	[5]

\*NA: Non-associative. \*\*2B: Associative type 2B.

### Supplementary A2. Methane ( $\text{CH}_4$ ) results

The first part of the development of the present work consisted of conducting tests with parameterizations indicated in the literature for the validation of the algorithm developed for estimating the parameters of ionic liquids. Thus, tests were performed with  $\text{CH}_4$ ,  $\text{CO}_2$ , and  $\text{H}_2\text{S}$ . The following figures show the results obtained for the EoS CPA and PC-SAFT  $\text{CH}_4$ ,  $\text{CO}_2$ , and  $\text{H}_2\text{S}$ . In summary, the algorithm proved to be able to be applied to ionic liquids. In addition, it is worth noting that the parameterizations applied to EoS for  $\text{CH}_4$ ,  $\text{CO}_2$ , and  $\text{H}_2\text{S}$  were obtained from the literature.

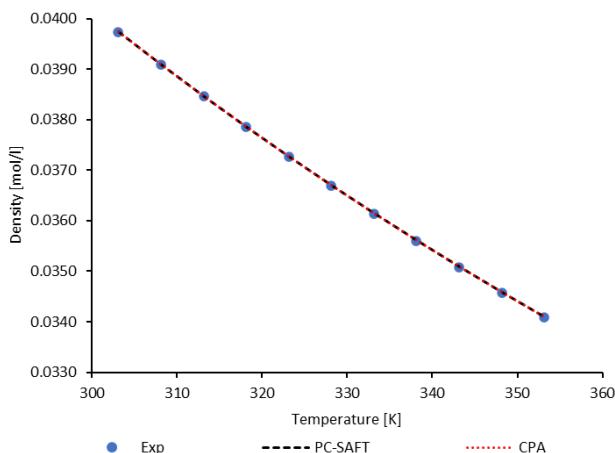


Figure S1. Density vs temperature data for  $\text{CH}_4$  calculated by CPA and PC-SAFT EoS. Experimental data from NIST [6].

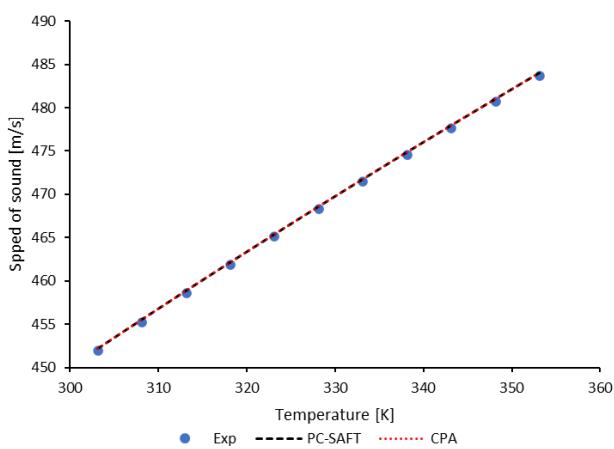


Figure S2. Speed of sound vs temperature data for  $\text{CH}_4$  calculated by CPA and PC-SAFT EoS. Experimental data from NIST [6].

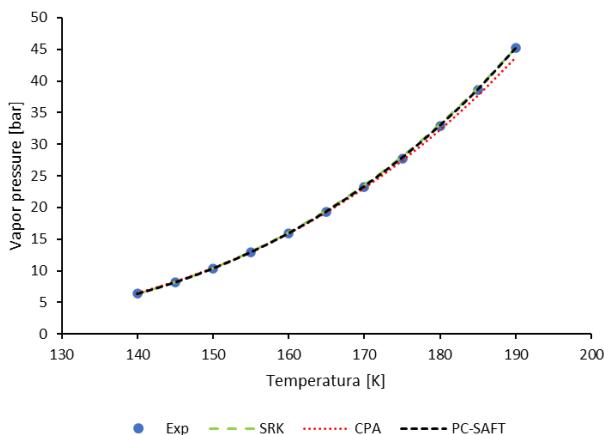


Figure S3. Vapor pressure vs temperature data for  $\text{CH}_4$  calculated by SRK, CPA, and PC-SAFT EoS. Experimental data from NIST [6].

### Supplementary A3. Carbon Dioxide ( $\text{CO}_2$ ) results

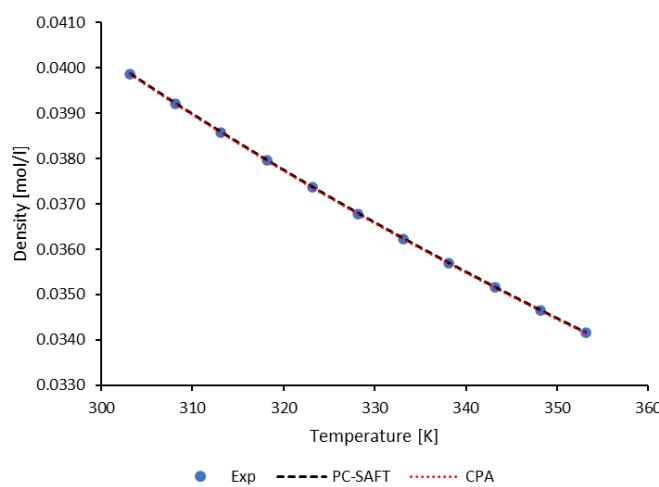


Figure S4. Density vs temperature data for  $\text{CO}_2$  calculated by CPA and PC-SAFT EoS. Experimental data from NIST [6].

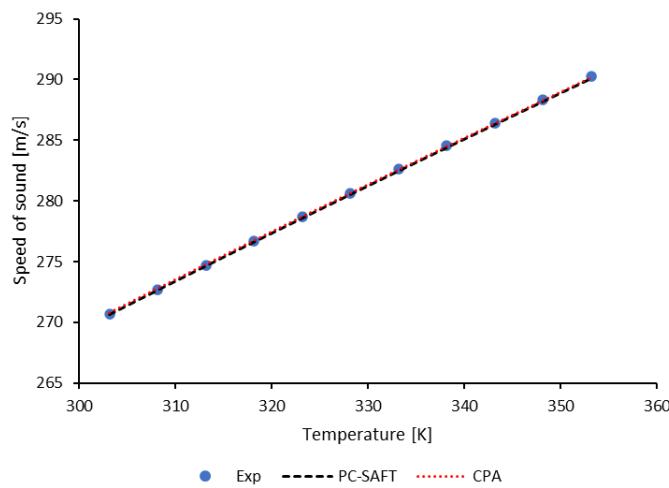


Figure S5. Speed of sound vs temperature data for  $\text{CO}_2$  calculated by CPA and PC-SAFT EoS. Experimental data from NIST [6].

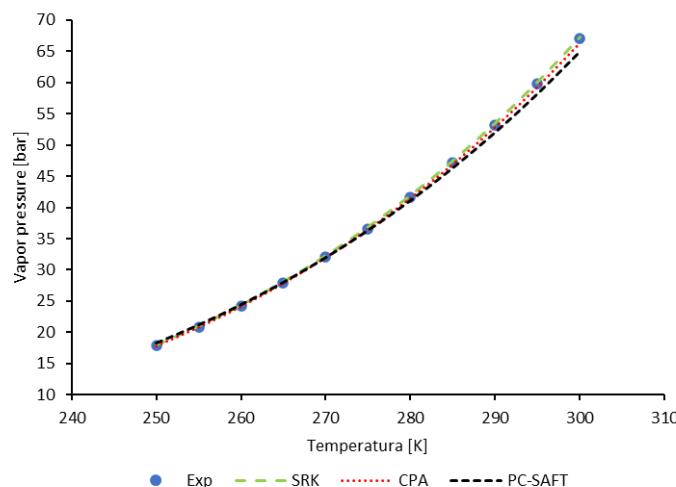


Figure S6. Vapor pressure vs temperature data for  $\text{CO}_2$  calculated by SRK, CPA, and PC-SAFT EoS. Experimental data from NIST [6].

### Supplementary A4. Hydrogen Sulfide ( $H_2S$ ) results

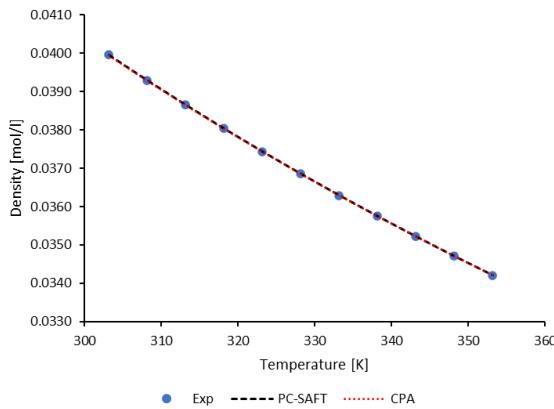


Figure S7. Density vs temperature data for  $H_2S$  calculated by CPA and PC-SAFT EoS. Experimental data from NIST [6].

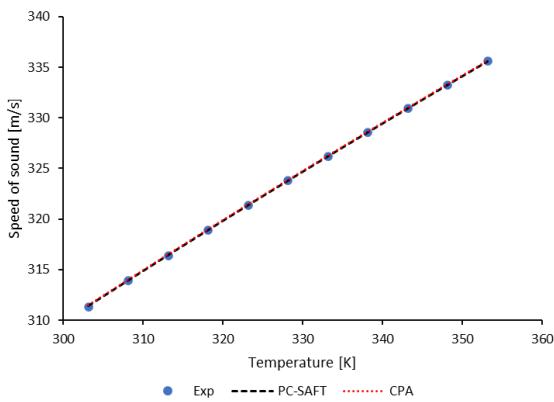


Figure S8. Density vs temperature data for  $H_2S$  calculated by CPA and PC-SAFT EoS. Experimental data from NIST [6].

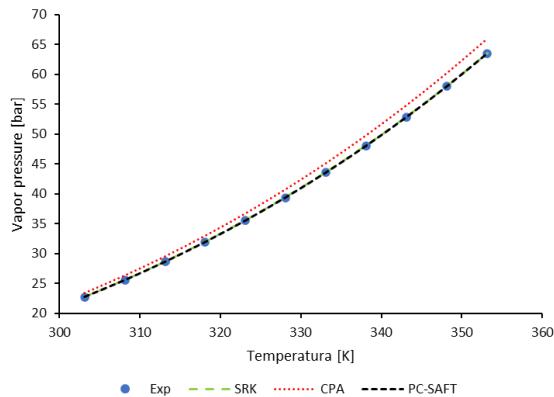


Figure S9. Vapor pressure vs temperature data for  $H_2S$  calculated by SRK, CPA, and PC-SAFT EoS. Experimental data from NIST [6].

### SUPPLEMENTARY B - Calculation memory from SRK EoS

This section presents the equations used to solve the SRK model.

#### Supplementary B1. Helmholtz free energy

The physical contribution of the Helmholtz energy is given by Equation (S-B1).

$$\tilde{a}^{\text{fs}} = -\ln(1-b\rho) - q(T)/(\rho) \quad (\text{S-B1})$$

where:

$$q(T) = \frac{a_0 \alpha(T)}{b R T} \quad (\text{S-B2})$$

$$I(\rho) = \frac{1}{\sigma - \varepsilon} \ln \left( \frac{1 + \sigma b \rho}{1 + \varepsilon b \rho} \right) \quad (\text{S-B3})$$

$$\alpha(T) = \left( 1 + c_1 \left( 1 - \sqrt{T_R} \right) \right)^2 \quad (\text{S-B4})$$

It is important to highlight that  $T$  and  $\rho$  are independent variables and the terms  $a_0$  and  $b$  are specific to each component. In addition,  $\sigma$  and  $\varepsilon$  are specific parameters of the equations of state, where they were obtained from Smith *et al.* [7].

### Supplementary B2. Compressibility factor (Z)

The calculation of pressure and fugacity coefficient is given by:

$$P = Z^{\text{fis}} \rho R T \quad (\text{S-B5})$$

$$\ln(\varphi) = \tilde{a}^{\text{res}} + Z^{\text{fis}} - 1 - \ln(Z^{\text{fis}}) \quad (\text{S-B6})$$

where:

$$Z^{\text{fis}} = \frac{1}{1 - b \rho} - \frac{q(T) b \rho}{(1 + \sigma b \rho)(1 + \varepsilon b \rho)} \quad (\text{S-B7})$$

### Supplementary B3. Derivative from the compressibility factor (Z) with respect to density ( $\rho$ )

$$\rho \frac{dZ^{\text{fis}}}{d\rho} = \frac{b \rho}{(1 - b \rho)^2} - \frac{q(T) b \rho (1 - \varepsilon \sigma b^2 \rho^2)}{[(1 + \sigma b \rho)(1 + \varepsilon b \rho)]^2} \quad (\text{S-B8})$$

### Supplementary B4. Derivative from the compressibility factor (Z) with respect to temperature (T)

$$T \frac{dZ^{\text{fis}}}{dT} = \frac{b \rho}{(1 + \sigma b \rho)(1 + \varepsilon b \rho)} q(T) (f_1 - 1) \quad (\text{S-B9})$$

where:

$$f_1 = T \frac{d \ln \alpha}{dT} = -c_1 \sqrt{\frac{T}{T_c \alpha(T)}} \quad (\text{S-B10})$$

### Supplementary B5. Speed of sound

$$u^{\text{fis}} = (f_1 - 1) q(T) I(\rho) \quad (\text{S-B11})$$

where:

$$u^{\text{res}} = u^{\text{fis}} \quad (\text{S-B12})$$

### Supplementary B6. Heat capacity at constant volume

$$C_V^{\text{fis}} = [(f_1 - 1)f_2 + f_2] q(T) I(\rho) \quad (\text{S-B13})$$

where:

$$f_2 = T \frac{d}{dT} \left( \frac{d \ln \alpha}{dT} \right) = T \frac{d^2 \ln \alpha}{dT^2} = -\frac{c_1}{2 \alpha(T)} \sqrt{T_R} \left( \sqrt{\alpha(T)} + c_1 \sqrt{T_R} \right) \text{ and} \quad (\text{S-B14})$$

$$C_V^{\text{res}} = C_V^{\text{fis}} \quad (\text{S-B15})$$

## SUPPLEMENTARY C - Calculation memory from CPA EoS

Supplementary C presents the equations used to solve the CPA model. It is worth noting that the contribution of the term physics is found in Supplementary B.

### Supplementary C1. Helmholtz free energy

The residual Helmholtz energy for the CPA equation of state is the sum of the Helmholtz energy of the resulting physical part of the SRK (Supplementary B) plus the associative Helmholtz energy, as shown in EoS (S-C1).

$$\bar{a}^{res} = \bar{a}^{fs} + \bar{a}^{assoc} \quad (\text{S-C1})$$

The associative Helmholtz energy is given by Equation (S-C2).

$$\bar{a}^{assoc} = \sum_{Ai} \left( \ln(X_{Ai}) + \frac{1-X_{Ai}}{2} \right) \quad (\text{S-C2})$$

Equation (S-C3) is a generalization of the equation proposed by Huang and Radosz (1990), which presents relationships between associative schemes 1A, 2B, 3B, and 4C.

$$X_{Ai} = \frac{-1 + \chi_3 \rho \Delta^{Ai Bj} + \sqrt{(1 + \chi_4 \rho \Delta^{Ai Bj})^2 + \chi_2 \rho \Delta^{Ai Bj}}}{\chi_1 \rho \Delta^{Ai Bj}} \quad (\text{S-C3})$$

*Table S4. Associative schemes of constants.*

Associative Schemes	$\chi_1$	$\chi_2$	$\chi_3$	$\chi_4$	Relation among $X_i$
1A	2	4	0	0	-
2B	2	4	0	0	$X_{Ai} = X_{Bi}$
3B	4	4	1	1	$X_{Ai} = X_{Bi}; X_{Ci} = 2.X_{Ai} - 1$
4C	4	8	0	0	$X_{Ai} = X_{Bi} = X_{Ci} = X_{Di}$

where:

$$\Delta^{Ai Bj} = g(V_m)^{ref} \left[ \exp \left( \frac{\varepsilon^{Ai Bj}}{RT} \right) - 1 \right] b_{ij} \beta^{Ai Bj} \quad (\text{S-C4})$$

$$\eta = \frac{b}{4 V_m} \quad (\text{S-C5})$$

$$g(V_m)^{ref} = \frac{1}{1 - 1.9 \eta} \quad (\text{S-C6})$$

## Supplementary C2. Compressibility factor (Z)

The calculation of the compressibility factor of the CPA equation of state is the sum of the compressibility factor of the physical part resulting from the SRK (Supplementary B) plus the associative compressibility factor (Equation S-C7).

$$Z = Z^{fs} + Z^{assoc} \quad (\text{S-C7})$$

The calculation of pressure and fugacity coefficient is given by:

$$P = Z \rho R T \quad (\text{S-C8})$$

$$\ln(\phi) = \bar{a}^{res} + Z - 1 - \ln(Z) \quad (\text{S-C9})$$

$$Z^{assoc} = -(1 + d_1) \frac{1}{2} \sum_{Ai} (1 - X_{Ai}) \quad (\text{S-C10})$$

where:

$$d_1 = \rho \frac{d \ln g}{d \rho} = \frac{1.9 \eta}{1 - 1.9 \eta} \quad (\text{S-C11})$$

## Supplementary C3. Derivative from the compressibility factor (Z) respect to density ( $\rho$ )

$$\rho \frac{dZ}{d\rho} = \rho \frac{dZ^{fs}}{d\rho} + \rho \frac{dZ^{assoc}}{d\rho} \quad (\text{S-C12})$$

$$\rho \frac{dZ^{assoc}}{d\rho} = \frac{-1.9 \eta}{(1 - 1.9 \eta)^2} \frac{1}{2} \sum_{Ai} (1 - X_{Ai}) + (1 + d_1) \frac{1}{2} \sum_{Ai} \rho_{Ai} \quad (\text{S-C13})$$

where:

$$\rho_{Ai} = \rho \frac{dX_{Ai}}{d\rho} = -\frac{\frac{1}{2} \left( \frac{\chi_2}{\chi_1} + \chi_3 + \chi_4 \right) - X_{Ai}}{1 + \rho \Delta^{Ai Bj} (X_{Ai} \chi_1 - \chi_3)} (1 + d_1) \quad (\text{S-C14})$$

### Supplementary C4. Derivative from the compressibility factor ( $Z$ ) with respect to ( $T$ )

$$T \frac{dZ}{dT} = T \frac{dZ^{fs}}{dT} + T \frac{dZ^{assoc}}{dT} \quad (\text{S-C15})$$

$$T \frac{dZ^{assoc}}{dT} = (1+d_1) \frac{1}{2} \sum_{Ai} (t_{Ai}) \quad (\text{S-C16})$$

where:

$$t_{Ai} = T \frac{dX_{Ai}}{dT} = q_1 \left[ \frac{0.5\chi_1 + (\rho \Delta^{Ai/Bj} \chi_4 + 1)\chi_4}{1 - (\chi_4 - X_{Ai}\chi_4)\rho \Delta^{Ai/Bj}} + \chi_3 - X_{Ai}\chi_1 \right] \frac{1}{\chi_1} \quad (\text{S-C17})$$

$$q_1 = -\frac{\exp\left(\frac{\varepsilon^{Ai/Bj}}{R T}\right) \frac{\varepsilon^{Ai/Bj}}{R T}}{\exp\left(\frac{\varepsilon^{Ai/Bj}}{R T}\right) - 1} \quad (\text{S-C18})$$

### Supplementary C5. Speed of sound

$$u^{res} = u^{fs} + u^{assoc} \quad (\text{S-C19})$$

The contribution of the associative speed of sound is given by Equation (S-C20).

$$u^{assoc} = \sum_{Ai} t_{Ai} g_{Ai} \quad (\text{S-C20})$$

where:

$$g_{Ai} = \sum_{Ai} \left( \frac{1}{2} - \frac{1}{X_{Ai}} \right) \quad (\text{S-C21})$$

### Supplementary C6. Heat capacity at constant volume

$$C_V^{res} = C_V^{fs} + C_V^{assoc} \quad (\text{S-C22})$$

The contribution of the associative heat capacity at constant volume is given by Equation (S-C23).

$$C_V^{assoc} = \sum_{Ai} L_{Ai} + \sum_{Ai} h_{Ai} g_{Ai} \quad (\text{S-C23})$$

where:

$$L_{Ai} = \left( \frac{t_{Ai}}{X_{Ai}} \right)^2 \quad (\text{S-C24})$$

$$h_{Ai} = T \frac{d}{dT} \left( T^2 \frac{dX_{Ai}}{dT} \right) = -\frac{V_{Ai}}{\Delta^{Ai/Bj}} \left[ t_{Ai} + G_1 - G_2 - \frac{1}{\chi_1} G_3 \right] - \frac{1}{\chi_1} G_4 G_5 \quad (\text{S-C25})$$

$$V_{Ai} = T \frac{d\Delta^{Ai/Bj}}{dT} = -b g(\rho) \beta^{Ai/Bj} \exp\left(\frac{\varepsilon^{Ai/Bj}}{R T}\right) \frac{\varepsilon^{Ai/Bj}}{R T} \quad (\text{S-C26})$$

$$G_1 = \frac{\left[ \rho \frac{V_1}{\chi_1} (X_{Ai}\chi_1 - \chi_3) + \rho t_{Ai} \Delta^{Ai/Bj} \right] \left[ 0.5 \chi_2 + (\rho \Delta^{Ai/Bj} \chi_4 + 1)\chi_4 \right]}{\left[ \rho (X_{Ai}\chi_1 - \chi_3) \Delta^{Ai/Bj} + 1 \right]^2} \quad (\text{S-C27})$$

$$G_2 = \frac{\rho \frac{V_{Ai}}{\chi_1} (\chi_4)^2}{\rho (X_{Ai}\chi_1 - \chi_3) \Delta^{Ai/Bj} + 1} \quad (\text{S-C28})$$

$$G_3 = \left[ \frac{0.5 \chi_2 + (\rho \Delta^{Ai/Bj} \chi_4 + 1)\chi_4}{1 - (\chi_3 - X_{Ai}\chi_1)} + \chi_3 - X_{Ai}\chi_1 \right] \quad (\text{S-C29})$$

$$G_4 = \left[ \frac{0.5 \chi_2 + (\rho \Delta^{Ai/Bj} \chi_4 + 1)\chi_4}{\rho (X_{Ai}\chi_1 - \chi_3) \Delta^{Ai/Bj} + 1} - X_{Ai}\chi_1 + \chi_3 \right] \quad (\text{S-C30})$$

$$G_5 = \left[ \frac{\frac{\varepsilon^{A_i B_j}}{R T} \exp\left(\frac{\varepsilon^{A_i B_j}}{R T}\right) \left(1 + \frac{\varepsilon^{A_i B_j}}{R T} - \exp\left(\frac{\varepsilon^{A_i B_j}}{R T}\right)\right)}{\left(\exp\left(\frac{\varepsilon^{A_i B_j}}{R T}\right) - 1\right)^2} \right] \quad (\text{S-C31})$$

## SUPPLEMENTARY D - Calculation memory from PC-SAFT EoS

Supplementary D presents the equations used to solve the PC-SAFT model.

$$\underline{\alpha}^{\text{res}} = \underline{\alpha}^{\text{hs}} + \underline{\alpha}^{\text{chain}} + \underline{\alpha}^{\text{disp}} + \underline{\alpha}^{\text{assoc}} \quad (\text{S-D1})$$

### Supplementary D1. Helmholtz free energy

The chain term is given by Equation S-D2:

$$\underline{\alpha}^{\text{chain}} = (1 - m_i) \ln(g_{ij}^{\text{hs}}(d_{ij})) \quad (\text{S-D2})$$

where the radial distribution function  $g_{ij}^{\text{hs}}(d_{ij})$ :

$$g_{ij}^{\text{hs}}(d_{ij}) = \frac{1 - 0.5 \eta}{(1 - \eta)^3} \quad (\text{S-D3})$$

The hard-sphere is given by Equation S-D4:

$$\underline{\alpha}^{\text{hs}} = m_i \frac{\eta (4 - 3\eta)}{(1 - \eta)^2} \quad (\text{S-D4})$$

where the coefficient  $\eta$  is:

$$\eta = \frac{\pi}{6} N_{av} \rho m_i (d_i(T))^3 \quad (\text{S-D5})$$

And the temperature-dependent segment diameter is:

$$d_i(T) = \delta_i \left[ 1 - 0.12 \exp\left(-\frac{3 \varepsilon_i}{k_B T}\right) \right] \quad (\text{S-D6})$$

The dispersive term is given by Equation S-D7:

$$\underline{\alpha}^{\text{disp}} = \underline{\alpha}_A^{\text{disp}} + \underline{\alpha}_B^{\text{disp}} \quad (\text{S-D7})$$

where:

$$\underline{\alpha}_A^{\text{disp}} = -2 \pi \rho I_1 m^2 N_{av} \sigma_{ij}^3 \left( \frac{\varepsilon_{ij}}{k_B T} \right) \quad (\text{S-D8})$$

$$\underline{\alpha}_B^{\text{disp}} = -\pi \rho \bar{m} C_1 I_2 m^2 N_{av} \sigma_{ij}^3 \left( \frac{\varepsilon_{ij}}{k_B T} \right) \quad (\text{S-D9})$$

$$C_1 = \left[ 1 + \bar{m} \frac{8\eta - 2\eta^2}{(1-\eta)^4} + (1 - \bar{m}) \frac{20\eta - 27\eta^2 + 12\eta^3 - 2\eta^4}{[(1-\eta)(2-\eta)]^2} \right]^{-1} \quad (\text{S-D10})$$

$$I_1 = \sum_{i=0}^6 \underline{\alpha}_i (\bar{m}) \eta^i \quad (\text{S-D11})$$

$$I_2 = \sum_{i=0}^6 b_i (\bar{m}) \eta^i \quad (\text{S-D12})$$

$$\underline{\alpha}_i (\bar{m}) = \underline{\alpha}_{0i} + \frac{\bar{m}-1}{\bar{m}} \underline{\alpha}_{1i} + \frac{\bar{m}-1}{\bar{m}} \frac{\bar{m}-2}{\bar{m}} \underline{\alpha}_{2i} \quad (\text{S-D13})$$

$$b_i (\bar{m}) = b_{0i} + \frac{\bar{m}-1}{\bar{m}} b_{1i} + \frac{\bar{m}-1}{\bar{m}} \frac{\bar{m}-2}{\bar{m}} b_{2i} \quad (\text{S-D14})$$

The associative term is given by Equation S-C2, as for the CPA EoS and the associative term  $X_{A_i}$  is given by Equation (S-C3), however, in PC-SAFT case the  $\Delta^{A_i B_j}$  is written as:

$$\Delta^{A_i B_j} = N_{av} \sigma_{ij}^3 g_{ij}^{\text{hs}}(d_{ij}) \left[ \exp\left(\frac{\varepsilon^{A_i B_j}}{k_B T}\right) - 1 \right] K^{A_i B_j} \quad (\text{S-D15})$$

### Supplementary D2. Compressibility factor (Z):

$$Z = Z^{hs} + Z^{chain} + Z^{disp} + Z^{assoc} \quad (\text{S-D16})$$

The hard-sphere is given by Equation S-D17:

$$Z^{hs} = 1 + m \frac{2\eta(2-\eta)}{(1-\eta)^3} \quad (\text{S-D17})$$

The chain term is given by Equation S-D18:

$$Z^{chain} = -(m-1) \frac{\eta(5-2\eta)}{(1-\eta)(2-\eta)} \quad (\text{S-D18})$$

The dispersive term is given by Equation S-D19:

$$Z^{disp} = Z_A^{disp} + Z_B^{disp} \quad (\text{S-D19})$$

where:

$$Z_A^{disp} = -2 \pi m^2 N_{av} \sigma_j^3 \left( \frac{\varepsilon_j}{kT} \right) \tilde{\rho} \frac{d}{d\eta} (\eta I_1) \quad (\text{S-D20})$$

$$Z_B^{disp} = -\pi m^3 N_{av} \sigma_j^3 \left( \frac{\varepsilon_j}{kT} \right)^2 \tilde{\rho} \left( C_1 \frac{d}{d\eta} (\eta I_2) \right) + C_2 \eta I_2 \quad (\text{S-D21})$$

$$\frac{d}{d\eta} (\eta I_1) = \sum_{i=0}^6 a_i(\bar{m}) (i+1) \eta^i \quad (\text{S-D22})$$

$$\frac{d}{d\eta} (\eta I_2) = \sum_{i=0}^6 b_i(\bar{m}) (i+1) \eta^i \quad (\text{S-D23})$$

$$C_2 = -C_1 \left[ m \frac{(8+20\eta-4\eta^2)}{(1-\eta)^5} + (1-m) \frac{(40-48\eta+12\eta^2+2\eta^3)}{[(1-\eta)(2-\eta)]^3} \right] \quad (\text{S-D24})$$

The associative term is given by Equation S-C8, in this case  $d_1$  is:

$$d_1 = \rho \frac{d \ln g}{d \rho} = \frac{\eta}{2-\eta} \frac{5-2\eta}{1-\eta} \quad (\text{S-E25})$$

### Supplementary D3. Derivative from the compressibility factor (Z) respect to density ( $\rho$ )

$$\rho \frac{dZ}{d\rho} = \rho \frac{dZ^{hs}}{d\rho} + \rho \frac{dZ^{chain}}{d\rho} + \rho \frac{dZ^{disp}}{d\rho} + \rho \frac{dZ^{assoc}}{d\rho} \quad (\text{S-E26})$$

The hard-sphere term is given by Equation S-D27:

$$\rho \frac{dZ^{hs}}{d\rho} = m \eta \frac{2(2+2\eta-\eta^2)}{(1-\eta)^4} \quad (\text{S-D27})$$

The hard-sphere term is given by Equation S-D28:

$$\rho \frac{dZ^{chain}}{d\rho} = -(m-1) \eta \left[ \frac{3}{(1-\eta)^2} - \frac{2}{(2-\eta)^2} \right] \quad (\text{S-D28})$$

The dispersive term is given by Equation S-D29:

$$\rho \frac{dZ^{disp}}{d\rho} = A + B C \quad (\text{S-D29})$$

where:

$$A = -2 \pi \tilde{\rho} I_1 m^2 N_{av} \sigma_j^3 \left( \frac{\varepsilon_j}{k_B T} \right) \frac{d}{d\eta} \left( \frac{\eta}{d\eta} \frac{I_1}{d\eta} \right) \quad (\text{S-D30})$$

$$B = -\pi N_{av} \tilde{\rho} \sigma_j^3 m^3 \left( \frac{\varepsilon_j}{k_B T} \right)^2 \quad (\text{S-D31})$$

$$C = 2 \eta C_2 \frac{d}{d\eta} (\eta I_2) + C_1 \frac{d}{d\eta} \left( \frac{\eta}{d\eta} \frac{I_2}{d\eta} \right) + \eta I_2 C_3 \quad (\text{S-D32})$$

$$C_3 = C_2 + \frac{2\eta C_2^2}{C_1} - C_1^2 \left[ m \frac{12\eta(5+6\eta-\eta^2)}{(1-\eta)^6} + (m-1) \frac{6\eta(\eta^4+8\eta^3-48\eta^2+80\eta-44)}{(\eta^2-3\eta+2)^4} \right] \quad (\text{S-D33})$$

$$\frac{d}{d\eta} \left( \frac{\eta}{d\eta} \frac{I_1}{d\eta} \right) = \sum_{i=0}^6 a_i(\bar{m}) (i+1)^2 \eta^i \quad (\text{S-D34})$$

$$\frac{d}{d\eta} \left( \frac{\eta}{d\eta} \frac{I_2}{d\eta} \right) = \sum_{i=0}^6 b_i(\bar{m}) (i+1)^2 \eta^i \quad (\text{S-D35})$$

The associative term is given by Equation S-D36:

$$\rho \frac{dZ_{assoc}}{d\rho} = N_1 \frac{1}{2} \sum_{Ai} (1 - X_{Ai}) + (1 + d_1) \frac{1}{2} \sum_{Ai} p_{Ai} \quad (\text{S-D36})$$

where:

$$N_1 = \left[ \frac{2\eta}{(2-\eta)^2} - \frac{3\eta}{(1-\eta)^2} \right] \quad (\text{S-D37})$$

The parameter  $d_1$  was obtained from Equation (S-D25),  $\eta$  from Equation (S-D5), and  $p_{Ai}$  from Equation (S-C14).

#### Supplementary D4. Derivative from the compressibility factor (Z) with respect to temperature (T)

$$T \frac{dZ}{dT} = T \frac{dZ^{hd}}{dT} + T \frac{dZ^{chain}}{dT} + T \frac{dZ^{disp}}{dT} + T \frac{dZ^{assoc}}{dT} \quad (\text{S-D38})$$

The hard-sphere term is given by Equation S-D39:

$$T \frac{dZ^{hs}}{dT} = -\rho \frac{dZ^{hs}}{dT} F_1 \quad (\text{S-D39})$$

where:

$$F_1 = \sigma_i \frac{1.08 \exp\left(-\frac{3\varepsilon_i}{k_B T}\right) \frac{3\varepsilon_i}{k_B T}}{d_i(T)} \quad (\text{S-D40})$$

The chain term is given by Equation S-D41:

$$T \frac{dZ^{chain}}{dT} = -\rho \frac{dZ^{chain}}{dT} F_1 \quad (\text{S-D41})$$

The dispersive term is given by Equation S-D42:

$$T \frac{dZ^{disp}}{dT} = -\alpha_A \frac{dZ^{disp}}{dT} \left[ F_1 \left[ \frac{d}{d\eta} \left( \eta I_1 \right) + F_1 \left( \frac{d}{d\eta} \left( \frac{\eta}{d\eta} \frac{I_1}{d\eta} \right) - \frac{d}{d\eta} \left( \eta I_1 \right) \right) \right] + F_2 [F_3 + F_1(F_4 + F_5)] \right] \quad (\text{S-D42})$$

where:

$$F_2 = \pi m^3 \rho N_{av} \sigma^3 \left( \frac{\varepsilon_i}{k_B T} \right)^2 \quad (\text{S-D43})$$

$$F_3 = 2 \left( C_1 \frac{d}{d\eta} (\eta I_2) + C_2 \eta I_2 \right) \quad (\text{S-D44})$$

$$F_4 = 2 C_2 \eta \frac{d}{d\eta} (\eta I_2) + C_1 \left( \frac{d}{d\eta} \left( \frac{\eta}{d\eta} \frac{I_2}{d\eta} \right) - \frac{d}{d\eta} (\eta I_2) \right) \quad (\text{S-D45})$$

$$F_5 = \eta I_2 (C_3 - C_2) \quad (\text{S-D46})$$

The associative term is given by Equation S-D47:

$$T \frac{dZ^{assoc}}{dT} = (1 + d_1) \frac{1}{2} \sum_{Ai} (t_{Ai}) - N_1 F_1 \frac{1}{2} \sum_{Ai} (1 - X_{Ai}) \quad (\text{S-D47})$$

where:

$$t_{Ai} = T \frac{dX_{Ai}}{dT} = [F_1 (1 + d_1) - N_2] N_3 \quad (\text{S-D48})$$

$$N_2 = \frac{\exp\left(\frac{\varepsilon^{Ai Bj} \beta^{Ai Bj}}{k_B T}\right) \frac{\varepsilon^{Ai Bj} \beta^{Ai Bj}}{k_B T}}{\exp\left(\frac{\varepsilon^{Ai Bj} \beta^{Ai Bj}}{k_B T}\right) - 1} \quad (\text{S-D49})$$

$$N_3 = \frac{1}{\chi_1} \left[ \frac{0.5 \chi_2 + (\rho \Delta \chi_4 + 1) \chi_4}{1 - (\chi_3 - X_{Ai} \chi_1) \rho \Delta} + \chi_3 - X_{Ai} \chi_1 \right] \quad (\text{S-D50})$$

#### Supplementary D5. Speed of sound

$$u_{res} = u_{hs} + u_{chain} + u_{disp} + u_{assoc} \quad (\text{S-D51})$$

The hard-sphere is given by Equation S-D52:

$$u_{hs} = F_1 (Z^{hs} - 1) \quad (\text{S-D52})$$

The chain term is given by Equation S-D53:

$$u_{chain} = F_1 Z^{chain} \quad (\text{S-D53})$$

The dispersive term is given by Equation S-D54:

$$\bar{u}^{\text{disp}} = \bar{a}_A [F_1 F_6 + 1] + \bar{a}_B (F_1 F_7 + 2) \quad (\text{S-D54})$$

where:

$$F_6 = \frac{\frac{d}{d\eta}(\eta I_1)}{I_1} - 1 \quad (\text{S-D55})$$

$$F_7 = \frac{C_2 \eta}{C_1} + \frac{\frac{d}{d\eta}(\eta I_2)}{I_2} - 1 \quad (\text{S-D56})$$

The associative term is given by Equation S-D57:

$$\bar{u}^{\text{assoc}} = \sum_{Ai} t_{Ai} J_{Ai} \quad (\text{S-D57})$$

where:

$$J_{Ai} = \frac{1}{2} - \frac{1}{X_{Ai}} \quad (\text{S-D58})$$

## Supplementary D6. Heat capacity at volume constant

$$\bar{C}_V^{\text{res}} = \bar{C}_V^{\text{hs}} + \bar{C}_V^{\text{chain}} + \bar{C}_V^{\text{disp}} + \bar{C}_V^{\text{assoc}} \quad (\text{S-D59})$$

The hard-sphere term is given by Equation S-D60:

$$\bar{C}_V^{\text{hs}} = (Z^{\text{hs}} - 1) F_8 + F_1 T \frac{dZ^{\text{hs}}}{dT} \quad (\text{S-D60})$$

where:

$$F_8 = \frac{3.24 \exp\left(-\frac{3 \varepsilon_i}{k_B T}\right) \frac{3 \varepsilon_i}{k_B T}}{\left[1 - 0.12 \exp\left(-\frac{3 \varepsilon_i}{k_B T}\right)\right]^2} \quad (\text{S-D61})$$

The chain term is given by Equation S-D62:

$$\bar{C}_V^{\text{chain}} = Z^{\text{chain}} F_8 + F_1 T \frac{dZ^{\text{chain}}}{dT} \quad (\text{S-D62})$$

The dispersive term is given by Equation S-D63:

$$\bar{C}_V^{\text{disp}} = \bar{C}_{V_1} + \bar{C}_{V_2} \quad (\text{S-D63})$$

where:

$$\bar{C}_{V_1} = -\bar{a}_A F_1 (F_6 F_{10} + F_9 F_1) \quad (\text{S-D64})$$

$$\bar{C}_{V_2} = -\bar{a}_B (F_1 F_7 + 2)(F_1 F_7 + 1) - F_1 F_7 F_{11} + F_1 F_{12} \quad (\text{S-D65})$$

$$F_9 = \frac{\frac{d}{d\eta} \left( \frac{\eta}{d\eta} \frac{I_1}{d\eta} \right)}{I_1} - 1 \quad (\text{S-D66})$$

$$F_{10} = \frac{-0.24 \exp\left(-\frac{3 \varepsilon_i}{k_B T}\right) \left(9 \frac{\varepsilon_i}{k_B T} + 1\right) + 2 - 3 \frac{\varepsilon_i}{k_B T}}{d_i(T)} \quad (\text{S-D67})$$

$$F_{11} = \sigma_i \frac{3 \frac{\varepsilon_i}{k_B T} - \frac{\sigma_i}{d_i(T)}}{d_i(T)} \quad (\text{S-D68})$$

$$F_{12} = \frac{C_2 \eta}{C_1} \left( \frac{C_3}{C_2} - \frac{C_2 \eta}{C_1} \right) + \frac{\frac{d}{d\eta} \left( \frac{\eta}{d\eta} \frac{I_2}{d\eta} \right)}{I_2} - \left( \frac{\frac{d}{d\eta}(\eta I_2)}{I_2} \right)^2 \quad (\text{S-D69})$$

The associative term is given by Equation S-D70:

$$\bar{C}_V^{\text{assoc}} = \sum_{Ai} L_{Ai} + \sum_{Ai} h_{Ai} J_{Ai} \quad (\text{S-D70})$$

Where is given by Equation S-C24 and:

$$h_{Ai} = \frac{d}{dT} \left( T^2 \frac{dX_{Ai}}{dT} \right) = -\frac{V_{Ai}}{\Delta^{Ai/Bj}} \left[ t_{Ai} + G_1 - G_2 - \frac{1}{\chi_1} G_3 \right] - \frac{1}{\chi_1} G_4 G_5 + G_6 \quad (\text{S-D71})$$

$$\nu_{Ai} = T \frac{d\Delta^{Ai/Bj}}{dT} = \Delta^{Ai/Bj} [F_1 (1+d_1) - N_2] \quad (\text{S-D72})$$

The terms  $G_1$  to  $G_5$  are given from equation (S-C27) to (S-C31) and

$$G_6 = F_1 \left[ \left( 3 \frac{\varepsilon_i}{k_B T} - 1 \right) (1+d_1) + F_1 N_1 \right] + G_7 \quad (\text{S-D73})$$

$$G_7 = \sigma_i^2 \frac{0.388 \left( \frac{\varepsilon_i}{k_B T} \right)^2 \exp \left( -6 \frac{\varepsilon_i}{k_B T} (1+d_1) \right)}{(d(T))^2} \quad (\text{S-D74})$$

## SUPPLEMENTARY E - Ionic liquids results

In Supplementary E are presented the estimated parameters for ionic liquids, constants of the  $C_p^{gi}$  equation, the absolute average relative deviations of the equations of state, and the corresponding curves for methane, acid gases, ionic liquids, and solubility between ILs and other mentioned components.

Time is a major factor for everyday applications, which is worth noting that the estimation time of the parameters of ionic liquids, in which [EMIM][TfO] presented an estimation duration of 9 min 28 s for SRK EoS and non-associative CPA.

On the other hand, the associative CPA presented an average time of 48 min (which showed differences with the use of the associative scheme and parameter) and the non-associative PC-SAFT presented a duration of 43 min 26 s, while the associative PC-SAFT had an average of 1 h 54 min.

Nevertheless, [OMIM][NTf<sub>2</sub>] presented an estimation duration of 23min33s for the SRK EoS and non-associative CPA, the average duration of 1 h 56 min for the CPA (which showed differences with the associative scheme and in the associative parameter) and the non-associative PC-SAFT had a duration of 2 h 40 min, while for the associative PC-SAFT it had an average of 5h05min. Furthermore, the Swarm method used to estimate the parameters was applied five hundred iterations and one hundred particles for all cases analyzed. In conclusion, the estimation time of the parameters of the studied EoS was shorter for the SRK and longer for the PC-SAFT, given the complexity of the resolution of these models. It is also worth noting that the estimation time increased according to the amount of experimental data, which could be seen by analyzing the mean times between the ionic liquids [EMIM][TfO] and [OMIM][NTf<sub>2</sub>] for the SRK, which were from 9 min 28 s and 23 min 33 s, respectively; associative CPA which were 48 min and 1 h 56 min, respectively; the non-associative PC-SAFT were 43min26s and 2 h 40 mins, respectively; and, finally, the associative PC-SAFT which lasted 1 h 54 min and 5 h 05 min. Thus, it is necessary to verify if the computational effort spent in estimating the parameters of the pure components favors the prediction of the solubilities of the components in ionic liquids.

For that, the algorithm for estimating the parameters of the equations of state was developed in the Visual Studio Code source code editor in Python programming language, using a computer with a 64-bit Windows 10 Home Single Language operating system, Intel processor® Core™ i5-8250U @1.60GHz CPU, 20.0GB @2133MHz RAM, Intel® UHD Graphics 620 processor graphics, 120GB SSD with reading speed up to 500MB/s and exclusive 1TB WDC HDD for storage.

### Supplementary E1. EoS parameters

Table S5. Parameters of the  $C_p^{gi}$  equation for the SRK and CPA EoS.

Components	$C_{1i}$	$C_{2i}$	$C_{3i}$	$C_{4i}$	$C_{5i}$	$\beta^{AB}$	Model
[EMIM][TfO]	1906.93	-3.00803	0.00243	-21816563	-334428		SRK*
	1812.39	-2.83041	0.00231	-20181062	-315543	1	(1A)
	746.07	-0.57261	0.00053	-2972734	-95732	1	(2B)
	746.07	-0.57261	0.00053	-2972734	-95732	0.1	(2B)
	746.07	-0.57261	0.00053	-2972734	-95732	0.001	(2B)
	746.07	-0.57261	0.00053	-2972734	-95732	0.00001	(2B)
	746.07	-0.57261	0.00053	-2972734	-95732	1	(3B)
[OMIM][NTf <sub>2</sub> ]	856.04	-0.78345	0.00068	-5707203	-128975	1	(4C)
	54380.38	-125.70758	0.11048	-728483247	-10291960		SRK*
	63033.30	-144.77432	0.12627	-861847080	-12051169	1	(1A)
	57646.83	-133.22209	0.11704	-777254751	-10953470	1	(2B)
	52323.73	-121.56937	0.10748	-695112161	-9873353	0.1	(2B)
	76296.58	-174.96182	0.15201	-1051597543	-14650452	0.001	(2B)
	60021.48	-137.94008	0.12045	-819419049	-11473963	0.00001	(2B)
	57646.83	-133.22209	0.11704	-777254751	-10953470	1	(3B)
	51619.99	-120.53575	0.10715	-681362527	-9724358	1	(4C)

\*SRK: Soave-Redlich-Kwong is the same for non-associative CPA.  $(C_p^{gi}, J \text{ mol}^{-1} K^{-1}) = C_{1i} + C_{2i}(T, K) + C_{3i}(T, K)^2 - \frac{C_{4i}}{(T, K)^2} + \frac{C_{5i}}{(T, K)}$

Table S6. Parameters of the  $C_p^{gi}$  equation for the PC-SAFT EoS.

Components	$C_{1i}$	$C_{2i}$	$C_{3i}$	$C_{4i}$	$C_{5i}$	$K^{AB}$	Model
[EMIM][TfO]	-2062.10	5.41885	-0.00422	39509475	441814		NA*
	51.23	0.94879	-0.00065	5509111	209	1	(1A)
	442.24	0.19566	-0.00010	-1130439	-86513	1	(2B)
	442.24	0.19566	-0.00010	-1130439	-86513	0.1	(2B)
	442.24	0.19566	-0.00010	-1130439	-86513	0.001	(2B)
	442.24	0.19566	-0.00010	-1130439	-86513	0.00001	(2B)
	8718.79	-17.58111	0.01420	-133361977	-1796310	1	(3B)
	81.01	1.12612	-0.00095	4304740	-20470	1	(4C)
	59836.51	-138.07784	0.12146	-801838185	-11334897		NA*
	55897.85	-129.29266	0.11415	-742967569	-10550518	1	(1A)
[OMIM][NTf <sub>2</sub> ]	56780.91	-131.10416	0.11557	-757683454	-10739526	1	(2B)
	56780.91	-131.10416	0.11557	-757683454	-10739526	0.1	(2B)
	86561.74	-195.15190	0.16719	-1233765944	-16890129	0.001	(2B)
	53592.67	-123.27552	0.10831	-717995147	-10159673	0.00001	(2B)
	61452.95	-141.27142	0.12386	-831036297	-11695363	1	(3B)
	58500.50	-134.55250	0.11817	-786883440	-11112937	1	(4C)
	58500.50	-134.55250	0.11817	-786883440	-11112937	1	(4C)
	58500.50	-134.55250	0.11817	-786883440	-11112937	1	(4C)
	58500.50	-134.55250	0.11817	-786883440	-11112937	1	(4C)

\* NA: Non-associative.  $\left(C_p^{gi}, J \text{ mol}^{-1} K^{-1}\right) = C_{1i} + C_{2i}(T, K) + C_{3i}(T, K)^2 - \frac{C_{4i}}{(T, K)^2} + \frac{C_{5i}}{(T, K)}$

Table S7. Estimated parameters of the ionic liquids from the RK-Aspen model.

Components	MM [g/mol]	T <sub>c</sub> [K]	P <sub>c</sub> * [bar]	$\omega$ [-]	Estimation time
[EMIM][TfO]	260.23	1217.53	49.742	0.01164	9 min 28 s
[OMIM][NTf <sub>2</sub> ]	475.47	581.50	12.287	2.44405	23 min 33 s

Table S8. Estimated parameters of the ionic liquids from CPA EoS.

Components	$\beta^{AB**}$ or $K^{AB***}$	Associative schemes	CPA	PC-SAFT
			Estimation time	Estimation time
[EMIM][TfO]		NA*	9 min 28 s	43 min 26 s
	1	1A	46 min 17 s	1 h 55 min
	1	2B	49 min 15 s	1 h 49 min
	0.1	2B	48 min 12 s	1 h 53 min
	0.001	2B	50 min 04 s	1 h 58 min
	0.00001	2B	50 min 35 s	1 h 54 min
	1	3B	46 min 26 s	1 h 56 min
	1	4C	45 min 15 s	1 h 51 min
		NA*	23 min 33 s	2 h 40 min
	1	1A	1 h 54 min	5 h 08 min
[OMIM][NTf <sub>2</sub> ]	1	2B	1 h 55 min	5 h 03 min
	0.1	2B	1 h 53 min	5 h 05 min
	0.001	2B	2 h 02 min	5 h 04 min
	0.00001	2B	1 h 58 min	5 h 02 min
	1	3B	1 h 56 min	5 h 09 min
	1	4C	1 h 57 min	5 h 03 min

\* NA: Non-associative. \*\*  $\beta^{AB}$ : for CPA EoS. \*\*\*  $K^{AB}$ : for PC-SAFT EoS.

Table S9. Regressed parameters in [SI] for [EMIM][TfO] (i) for CH<sub>4</sub>, CO<sub>2</sub>, and H<sub>2</sub>S (j) with the RK-Aspen model.

[EMIM][TfO] / CH <sub>4</sub>				
Parameters	$k_{aij}^0$	$k_{aij}^1 \left[\frac{1}{T}\right]$	$k_{bij}^0$	$k_{bij}^1$
2p	0.05696	0	0.00570	0
	-0.00168	0.11650	-0.06598	0.20602
[EMIM][TfO] / CO <sub>2</sub>				
Parameters	$k_{aij}^0$	$k_{aij}^1 \left[\frac{1}{T}\right]$	$k_{bij}^0$	$k_{bij}^1$
2p	0.09333	0	0.03200	0
	0.13593	-0.19652	-0.01032	0.10532
[EMIM][TfO] / H <sub>2</sub> S				
Parameters	$k_{aij}^0$	$k_{aij}^1 \left[\frac{1}{T}\right]$	$k_{bij}^0$	$k_{bij}^1$
2p	0.03711	0	0.03236	0
	0.11858	-0.25830	0.07277	-0.12887

$$a_{ij} = \sqrt{a_i a_j} \left( 1 - k_{aij}^0 - k_{aij}^1 \frac{T}{1000} \right); b_{ij} = \frac{b_i + b_j}{2} \left( 1 - k_{bij}^0 - k_{bij}^1 \frac{T}{1000} \right).$$

Table S10. Regressed parameters in [SI] for [OMIM][NTf<sub>2</sub>] (i) for CO<sub>2</sub> and H<sub>2</sub>S (j) with the RK-Aspen model.

[OMIM][NTf <sub>2</sub> ] / CO <sub>2</sub>				
Parameters	k <sub>aij</sub> <sup>0</sup>	k <sub>aij</sub> <sup>1</sup> [1/T]	k <sub>bij</sub> <sup>0</sup>	k <sub>bij</sub> <sup>1</sup>
2p	-0.05199	0	0.02328	0
4p	0.48683	-1.68080	0.03427	-0.04782
[OMIM][NTf <sub>2</sub> ] / H <sub>2</sub> S				
Parameters	k <sub>aij</sub> <sup>0</sup>	k <sub>aij</sub> <sup>1</sup> [1/T]	k <sub>bij</sub> <sup>0</sup>	k <sub>bij</sub> <sup>1</sup>
2p	-0.04887	0	0.02357	0
4p	0.36222	-1.28246	0.00886	0.02947

$$a_{ij} = \sqrt{a_i a_j} \left( 1 - k_{aij}^0 - k_{aij}^1 \frac{T}{1000} \right); b_{ij} = \frac{b_i + b_j}{2} \left( 1 - k_{bij}^0 - k_{bij}^1 \frac{T}{1000} \right)$$

Table S11. Regressed parameters in [SI] for [EMIM][TfO] (i) and CH<sub>4</sub> (j) with CPA and PC-SAFT models with different associative schemes of the ionic liquid for β<sup>AB</sup> e K<sup>AB</sup> equal to one.

CPA										
Schemes	NA*		1A		2B		3B		4C	
Parameters	k <sub>ij</sub> <sup>0</sup>	k <sub>ij</sub> <sup>1</sup>								
1p	0.08275	0	0.07917	0	0.07381	0	0.07381	0	0.06022	0
2p	0.16636	-0.07751	0.16935	-0.08361	0.16675	-0.08619	0.16675	-0.08619	0.21052	-0.13943
PC-SAFT										
Schemes	NA*		1A		2B		3B		4C	
Parameters	k <sub>ij</sub> <sup>0</sup>	k <sub>ij</sub> <sup>1</sup>								
1p	-0.10359	0	-0.10292	0	-0.10271	0	-0.10271	0	-0.10203	0
2p	0.06731	-0.09611	0.04432	-0.15865	0.02092	-0.06952	0.02092	-0.06953	-0.02364	-0.04409

$$* \text{ NA: Non-associative. CPA: } k_{ij} = k_{ij}^0 + k_{ij}^1 \frac{T}{298.15K}. \text{ PC-SAFT: } k_{ij} = k_{ij}^0 + \frac{k_{ij}^1}{T_r}.$$

Table S12. Regressed parameters in [SI] for [EMIM][TfO] (i) and CO<sub>2</sub> (j) with CPA and PC-SAFT models with different associative schemes of the ionic liquid for β<sup>AB</sup> e K<sup>AB</sup> equal to one.

CPA										
Schemes	NA*		1A		2B		3B		4C	
Parameters	k <sub>ij</sub> <sup>0</sup>	k <sub>ij</sub> <sup>1</sup>								
1p	0.03019	0	0.01586	0	-0.00067	0	-0.00067	0	-0.04226	0
2p	0.19635	-0.15320	0.20084	-0.17057	0.20893	-0.19330	0.20893	-0.19330	0.24176	-0.26203
PC-SAFT										
Schemes	NA*		1A		2B		3B		4C	
Parameters	k <sub>ij</sub> <sup>0</sup>	k <sub>ij</sub> <sup>1</sup>								
1p	0.01917	0	0.00925	0	-0.00031	0	-0.00031	0	-0.01799	0
2p	0.04450	-0.02742	0.02403	-0.01601	0.00329	-0.00390	0.00329	-0.00390	-0.03734	0.02098

$$* \text{ NA: Non-associative. CPA: } k_{ij} = k_{ij}^0 + k_{ij}^1 \frac{T}{298.15K}. \text{ PC-SAFT: } k_{ij} = k_{ij}^0 + \frac{k_{ij}^1}{T_r}.$$

Table S13. Regressed parameters in [SI] for [EMIM][TfO] (i) and CO<sub>2</sub> (j) with CPA and PC-SAFT models with different associative parameters of the ionic liquid for NA and 2B scheme.

CPA										
Schemes	NA*		β <sup>AB</sup> =1		β <sup>AB</sup> =0.1		β <sup>AB</sup> =0.001		β <sup>AB</sup> =0.00001	
Parameters	k <sub>ij</sub> <sup>0</sup>	k <sub>ij</sub> <sup>1</sup>								
1p	0.03019	0	-0.00067	0	-0.00067	0	-0.00067	0	-0.00066	0
2p	0.19635	-0.15320	0.20893	-0.19330	0.20893	-0.19330	0.20891	-0.19328	0.20869	-0.19307
PC-SAFT										
Schemes	NA*		K <sup>AB</sup> =1		K <sup>AB</sup> =0.1		K <sup>AB</sup> =0.001		K <sup>AB</sup> =0.00001	
Parameters	k <sub>ij</sub> <sup>0</sup>	k <sub>ij</sub> <sup>1</sup>								
1p	0.01917	0	-0.00031	0	-0.00033	0	-0.00032	0	-0.00032	0
2p	0.04450	-0.02742	0.00329	-0.00390	0.00326	-0.00390	0.00327	-0.00390	0.00328	-0.00390

$$* \text{ NA: Non-associative. CPA: } k_{ij} = k_{ij}^0 + k_{ij}^1 \frac{T}{298.15K}. \text{ PC-SAFT: } k_{ij} = k_{ij}^0 + \frac{k_{ij}^1}{T_r}.$$

**Table S14.** Regressed parameters in [SI] for [EMIM][TfO] (*i*) and H<sub>2</sub>S (*j*) with CPA and PC-SAFT models with different associative schemes of the ionic liquid for  $\beta_{AB}^0$  e  $K_{AB}^0$  equal to one.

Schemes Parameters	CPA									
	k <sub>ij</sub> <sup>0</sup>	k <sub>ij</sub> <sup>1</sup>	1A		2B		3B		4C	
1p	-0.11494	0	0.03387	0	0.04658	0	NR**	NR**	0.10690	0
2p	0.16053	-0.25611	-0.13650	0.15839	-0.02072	0.06258	NR**	NR**	-0.00065	0.10010
PC-SAFT										
Schemes Parameters	NA*									
	k <sub>ij</sub> <sup>0</sup>	k <sub>ij</sub> <sup>1</sup>								
1p	-0.00577	0	-0.00913	0	-0.01831	0	0.53917	0	-0.03218	0
2p	-0.01078	0.00536	-0.01923	0.01083	-0.03301	0.01577	0.35696	0.20056	-0.05642	0.02605

\* NA: Non-associative. \*\* NR: No results. CPA:  $k_{ij} = k_{ij}^0 + k_{ij}^1 \frac{T}{T_{ref}} = 298.15K$ . PC-SAFT:  $k_{ij} = k_{ij}^0 + \frac{k_{ij}^1}{T_r}$ .

**Table S15.** Regressed parameters in [SI] for [EMIM][TfO] (*i*) and H<sub>2</sub>S (*j*) with CPA and PC-SAFT models with different associative parameters of the ionic liquid for NA and 2B scheme.

Schemes Parameters	CPA									
	k <sub>ij</sub> <sup>0</sup>	k <sub>ij</sub> <sup>1</sup>	$\beta_{AB}^0=1$		$\beta_{AB}^0=0.1$		$\beta_{AB}^0=0.001$		$\beta_{AB}^0=0.00001$	
1p	-0.11494	0	0.04658	0	0.04658	0	0.04658	0	0.04656	0
2p	0.16053	-0.25611	-0.02072	0.06258	-0.02072	0.06257	-0.02069	0.06255	-0.02049	0.06234
PC-SAFT										
Schemes Parameters	NA*									
	k <sub>ij</sub> <sup>0</sup>	k <sub>ij</sub> <sup>1</sup>								
1p	-0.00577	0	-0.01831	0	-0.01833	0	-0.01832	0	-0.01832	0
2p	-0.01078	0.00536	-0.03301	0.01577	-0.03302	0.01576	-0.03302	0.01577	-0.03302	0.01576

**Table S16.** Regressed parameters in [SI] for [OMIM][NTf<sub>2</sub>] (*i*) and CO<sub>2</sub> (*j*) with CPA and PC-SAFT models with different associative schemes of the ionic liquid for  $\beta_{AB}^0$  e  $K_{AB}^0$  equal to one.

Schemes Parameters	CPA									
	k <sub>ij</sub> <sup>0</sup>	k <sub>ij</sub> <sup>1</sup>	1A		2B		3B		4C	
1p	-0.12307	0	-0.14721	0	-0.17441	0	-0.17441	0	-0.24057	
2p	0.34902	-0.42693	0.40481	-0.49940	0.47435	-0.58717	0.47435	-0.58717	0.67256	-0.82728
PC-SAFT										
Schemes Parameters	NA*									
	k <sub>ij</sub> <sup>0</sup>	k <sub>ij</sub> <sup>1</sup>								
1p	0.00989	0	0.00256	0	-0.00464	0	-0.00464	0	-0.01899	0
2p	-0.05048	0.06685	-0.06784	0.07799	-0.08525	0.08932	-0.08525	0.08932	-0.12003	0.11202

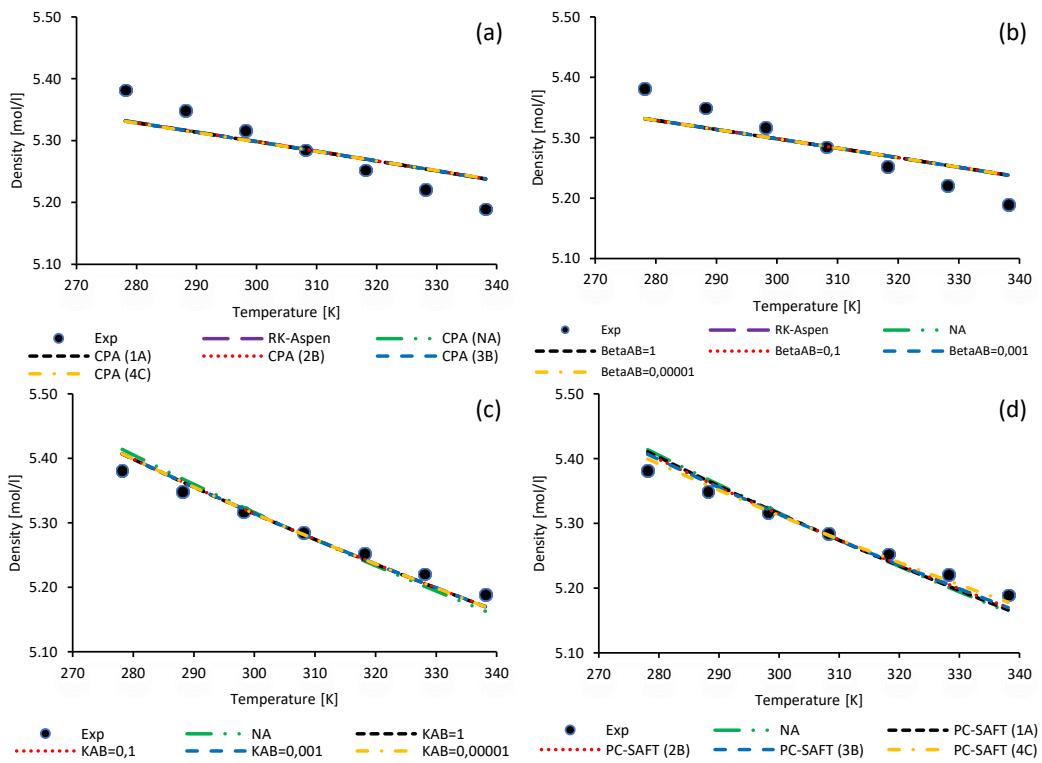
\* NA: Non-associative. CPA:  $k_{ij} = k_{ij}^0 + k_{ij}^1 \frac{T}{T_{ref}} = 298.15K$ . PC-SAFT:  $k_{ij} = k_{ij}^0 + \frac{k_{ij}^1}{T_r}$ .

**Table S17.** Regressed parameters in [SI] for [OMIM][NTf<sub>2</sub>] (*i*) and H<sub>2</sub>S (*j*) with CPA and PC-SAFT models with different associative schemes of the ionic liquid for  $\beta_{AB}^0$  e  $K_{AB}^0$  equal to one.

Schemes Parameters	CPA									
	k <sub>ij</sub> <sup>0</sup>	k <sub>ij</sub> <sup>1</sup>								
1p	-0.26137	0	-0.00097		-0.01580	0	NR**	NR**	0.05242	0
2p	0.40446	-0.60235	0.06721	-0.06165	0.18585	-0.18257	NR**	NR**	0.21765	-0.14976
PC-SAFT										
Schemes Parameters	NA*									
	k <sub>ij</sub> <sup>0</sup>	k <sub>ij</sub> <sup>1</sup>								
1p	-0.00103	0	-0.00199	0	-0.00755	0	0.76330	0	-0.01547	0
2p	-0.08395	0.09168	-0.09157	0.09906	-0.10371	0.10634	1.13283	-0.39925	-0.12417	0.12026

\* NA: Non-associative. \*\* NR: No results. CPA:  $k_{ij} = k_{ij}^0 + k_{ij}^1 \frac{T}{T_{ref}} = 298.15K$ . PC-SAFT:  $k_{ij} = k_{ij}^0 + \frac{k_{ij}^1}{T_r}$ .

### Supplementary E2. Properties calculation of pure ILs



**Figure S10.** Density vs temperature results for  $[EMIM][TfO]$ ; (a) Results for the RK-Aspen model and the non-associative CPA and with different associative schemes; (b) Results for different associative parameters for CPA EoS; (c) Results for different associative parameters for PC-SAFT EoS; (d) Results for the non-associative PC-SAFT and with different associative schemes. Experimental data from Vercher *et al.* [9].

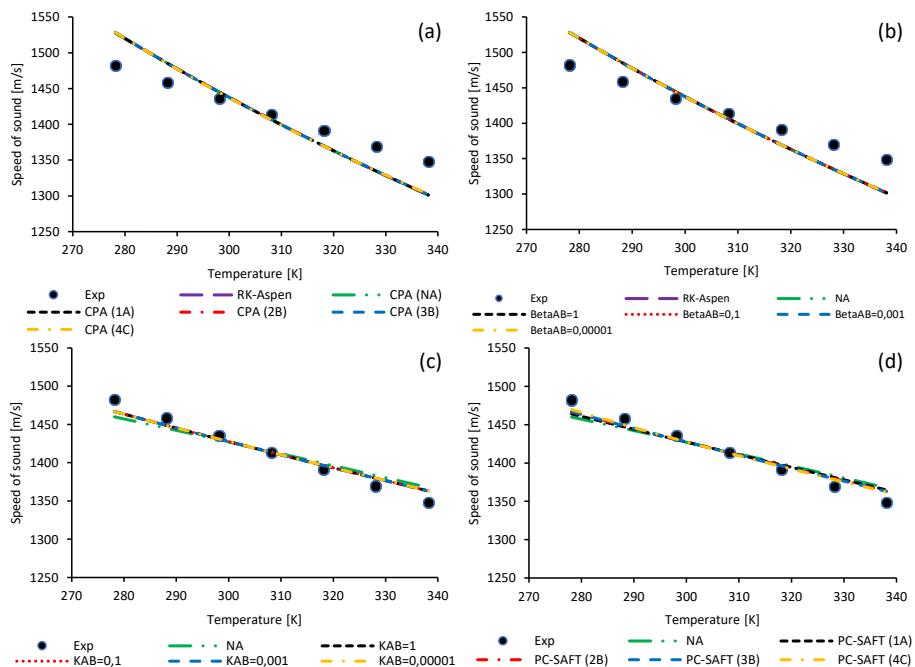


Figure S11. Speed of sound vs temperature results for [EMIM][TfO]: (a) Results for the RK-Aspen model and the non-associative CPA and with different associative schemes; (b) Results for different associative parameters for CPA EoS; (c) Results for different associative parameters for PC-SAFT EoS; (d) Results for the non-associative PC-SAFT and with different associative schemes. Experimental data from Vercher *et al.* [9].

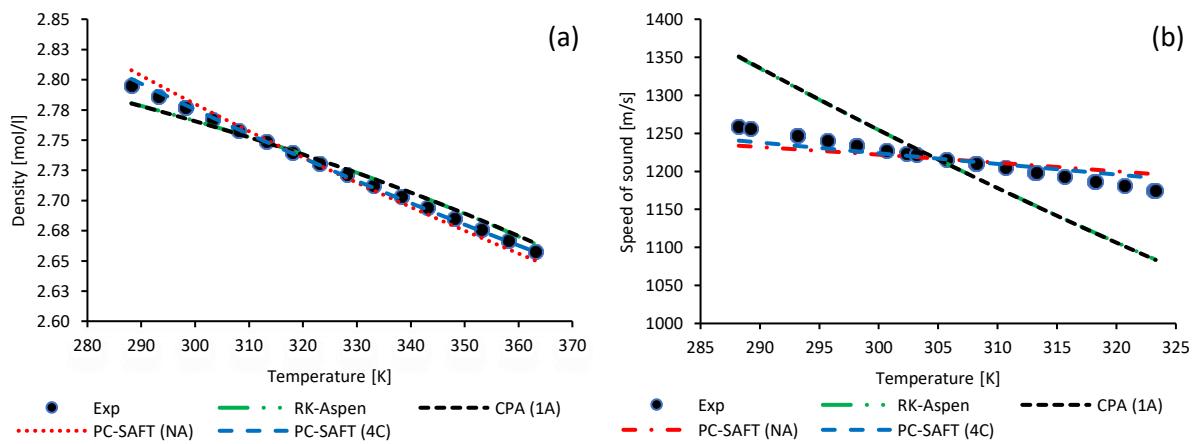


Figure S12. Density and speed of sound results for the RK-Aspen, CPA, and PC-SAFT models. Experimental data from Zorebski *et al.* [10].

### Supplementary E3. Methane ( $\text{CH}_4$ ) with [EMIM][TfO] results

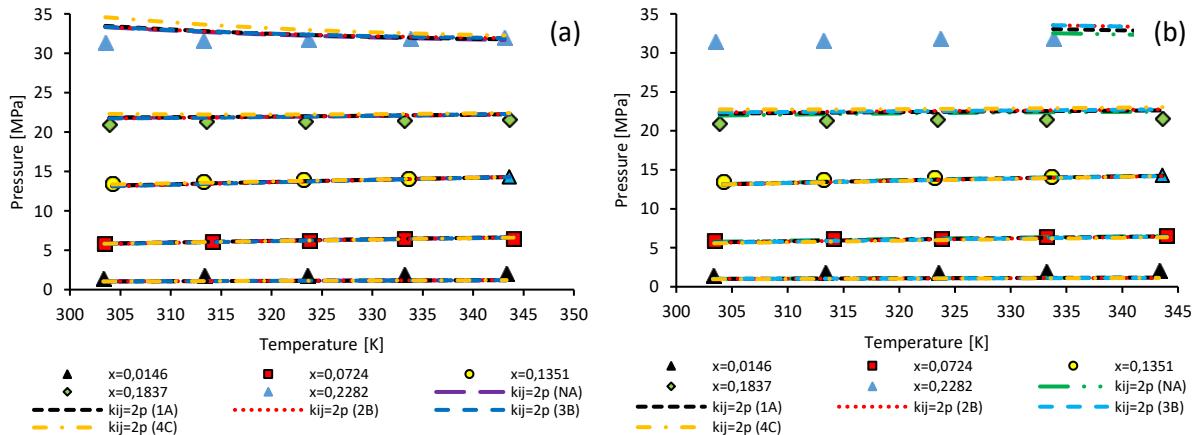


Figure S13. P-T results for  $\text{CH}_4$  and [EMIM][TfO]: (a) Results for CPA EoS with  $k_{ij}=2p$  for different associative schemes; (b) Results for PC-SAFT EoS with  $k_{ij}=2p$  for different associative schemes. Experimental data from Lee [11].

Table S18. Deviations in pressure for  $\text{CH}_4$  and [EMIM][TfO] using the RK-Aspen model.

$x_{\text{CH}_4}$	$k_{ij}=0$	$k_{ij}=2p$	$k_{ij}=4p$
0.0146	48.16	41.12	40.78
0.0724	20.60	9.26	2.79
0.1351	26.03	8.39	1.18
0.1837	27.26	11.82	2.68
0.2282	32.15	6.93	2.89
Average deviation (AARD)	23.02	11.50	8.54
$AARD(\%) = \frac{1}{n} \sum_{i=1}^n \left  \frac{p_i^{\text{exp}} - p_i^{\text{cal}}}{p_i^{\text{exp}}} \right  \times 100$			

Table S19. Deviations in pressure for  $\text{CH}_4$  and  $[\text{EMIM}][\text{TfO}]$  using the CPA and PC-SAFT EoS.

$x_{\text{CH}_4}$	CPA														
	$k_{ij}=0$				$k_{ij}=1p$				$k_{ij}=2p$						
	NA	1A	2B	3B	4C	NA	1A	2B	3B	4C	NA	1A	2B	3B	4C
0.0146	59.21	58.22	57.01	57.01	53.71	40.48	40.70	41.05	41.05	41.21	41.40	41.59	41.76	41.76	42.06
0.0724	38.06	36.31	34.17	34.17	28.39	4.18	4.08	4.43	4.43	4.96	1.49	1.37	1.89	1.89	1.41
0.1351	43.80	41.90	39.56	39.56	33.17	5.20	5.37	5.91	5.91	5.91	2.23	2.30	2.75	2.75	1.67
0.1837	46.06	43.89	41.22	41.22	33.75	6.93	7.26	7.46	7.46	9.99	4.14	4.33	3.79	3.79	6.46
0.2282	50.83	48.47	45.55	45.55	37.24	3.22	3.80	4.26	4.26	7.53	5.99	6.49	6.10	6.10	9.96
AARD	42.42	40.49	38.09	38.09	31.35	9.60	9.77	9.91	9.91	10.78	8.99	9.12	9.24	9.24	9.74

$x_{\text{CH}_4}$	PC-SAFT														
	$k_{ij}=-0.1$				$k_{ij}=1p$				$k_{ij}=2p$						
	NA	1A	2B	3B	4C	NA	1A	2B	3B	4C	NA	1A	2B	3B	4C
0.0146	35.78	37.29	38.31	38.31	40.16	38.11	39.13	39.99	39.99	41.38	38.47	39.40	40.19	40.19	41.48
0.0724	7.68	5.98	4.90	4.90	3.61	7.14	6.12	5.50	5.50	4.81	1.34	2.33	3.17	3.17	4.51
0.1351	9.86	7.91	6.37	6.37	3.70	8.99	7.61	6.30	6.30	3.87	1.49	1.71	1.87	1.87	2.06
0.1837	27.33	26.62	12.67	12.67	11.28	12.18	10.78	9.41	9.41	7.67	4.31	5.07	5.79	5.79	7.09
0.2282	62.64	61.69	61.17	61.17	80.39	64.79	63.49	62.21	62.21	60.78	60.59	61.27	61.89	61.89	81.38
AARD *	20.16	19.45	15.56	15.56	14.69	16.60	15.91	15.30	15.30	14.43	11.40	12.13	12.76	12.76	13.79

\* These data were performed disregarding  $x_{\text{CH}_4} = 0.2282$ .

#### Supplementary E4. Carbon Dioxide ( $\text{CO}_2$ ) with ionic liquids results

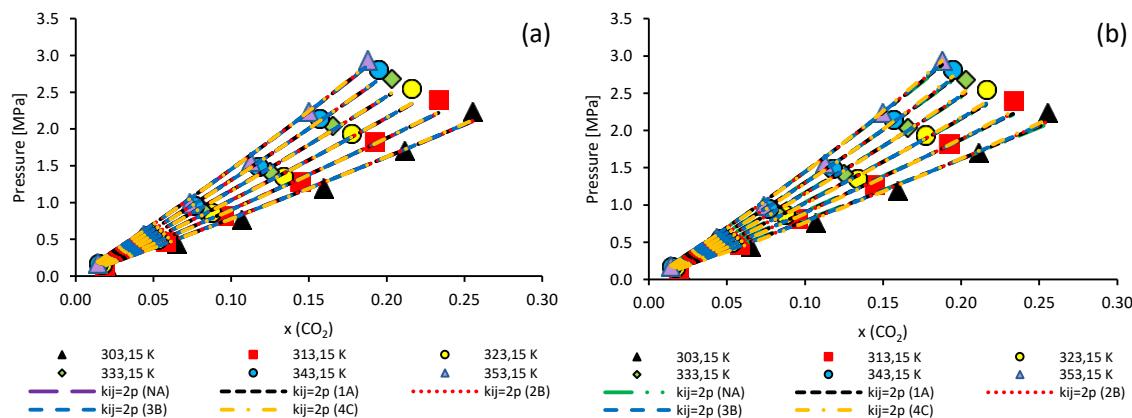


Figure S14.  $P$ - $x$  results for  $\text{CO}_2$  and  $[\text{EMIM}][\text{TfO}]$ : (a) Results for CPA EoS with  $k_{ij}=2p$  for different associative schemes; (b) Results for PC-SAFT EoS with  $k_{ij}=2p$  for different associative schemes. Experimental data from Nematpour *et al.* [12].

Table S20. Deviations in pressure for  $\text{CO}_2$  and  $[\text{EMIM}][\text{TfO}]$  using the RK-Aspen model.

Temperature [K]	$\text{CO}_2$		
	$k_{ij}=0$	$k_{ij}=2p$	$k_{ij}=4p$
303.15	10.50	5.05	3.16
313.15	8.25	4.61	1.38
323.15	5.39	3.31	2.26
333.15	3.82	2.53	2.45
343.15	4.98	4.05	1.41
353.15	9.36	8.81	2.38
AARD	7.05	4.69	2.17

*Table S21. Deviations in pressure for CO<sub>2</sub> and [EMIM][TfO] using the CPA and PC-SAFT EoS.*

Temperature [K]	CPA						k <sub>ij</sub> =1p						k <sub>ij</sub> =2p					
	NA	1A	2B	3B	4C	NA	1A	2B	3B	4C	NA	1A	2B	3B	4C			
303.15	18.71	11.12	4.81	4.81	21.51	5.22	5.01	4.79	4.79	5.65	7.95	7.73	7.52	7.52	7.12			
313.15	17.08	9.46	4.80	4.80	23.47	5.24	4.97	4.78	4.78	4.66	6.51	6.30	6.08	6.08	5.65			
323.15	14.90	7.19	5.34	5.34	26.25	5.59	5.39	5.20	5.20	4.81	5.61	5.42	5.22	5.22	4.81			
333.15	12.21	4.64	6.24	6.24	29.75	5.36	5.94	5.97	5.97	6.25	4.85	4.67	4.49	4.49	4.12			
343.15	8.27	3.71	9.39	9.39	35.11	8.15	8.51	9.01	9.01	10.62	4.75	4.59	4.42	4.42	4.10			
353.15	3.99	5.36	14.58	14.58	41.36	12.74	13.35	14.20	14.20	16.84	5.15	5.01	4.87	4.87	4.63			
AARD	12.53	6.91	7.53	7.53	29.57	7.15	7.19	7.33	7.33	8.14	5.81	5.62	5.43	5.43	5.07			
PC-SAFT																		
Temperature [K]	k <sub>ij</sub> =0						k <sub>ij</sub> =1p						k <sub>ij</sub> =2p					
	NA	1A	2B	3B	4C	NA	1A	2B	3B	4C	NA	1A	2B	3B	4C			
303.15	19.01	7.34	7.61	7.61	34.89	10.79	8.99	7.26	7.26	4.31	8.82	7.86	6.99	6.99	5.45			
313.15	21.18	9.49	5.64	5.64	31.57	7.64	6.51	5.46	5.46	3.53	7.16	6.24	5.39	5.39	3.86			
323.15	22.54	11.03	4.55	4.55	29.66	5.89	5.11	4.38	4.38	3.05	5.91	5.12	4.38	4.38	3.05			
333.15	23.23	11.79	3.62	3.62	28.90	4.42	3.92	3.46	3.46	2.64	4.83	4.15	3.52	3.52	2.46			
343.15	22.66	11.10	3.37	3.37	30.29	3.70	3.44	3.22	3.22	3.00	4.44	3.86	3.32	3.32	2.32			
353.15	21.48	9.71	3.73	3.73	32.70	3.53	3.49	3.49	3.49	5.23	4.56	4.08	3.72	3.72	3.08			
AARD	21.68	10.08	4.75	4.75	31.33	5.99	5.24	4.54	4.54	3.63	5.95	5.22	4.55	4.55	3.37			

*Table S22. Deviations in pressure for CO<sub>2</sub> and [OMIM][NTf<sub>2</sub>] using the RK-Aspen model.*

Temperature [K]	CO <sub>2</sub>		
	k <sub>ij</sub> =0	k <sub>ij</sub> =2p	k <sub>ij</sub> =4p
303.15	57.81	17.39	1.44
313.15	63.18	11.26	1.00
323.15	68.08	5.23	1.01
333.15	73.25	1.75	1.06
343.15	77.87	7.57	0.89
353.15	83.79	15.08	1.32
AARD	70.66	9.71	1.12

*Table S23. Deviations in pressure for CO<sub>2</sub> and [OMIM][NTf<sub>2</sub>] using the CPA and PC-SAFT EoS.*

Temperature [K]	CPA						k <sub>ij</sub> =1p						k <sub>ij</sub> =2p					
	NA	1A	2B	3B	4C	NA	1A	2B	3B	4C	NA	1A	2B	3B	4C			
303.15	53.56	66.11	80.48	80.47	116.35	16.68	18.60	20.75	20.75	25.91	7.48	7.42	7.36	7.36	7.30			
313.15	58.43	71.62	86.81	86.81	125.15	10.71	11.98	13.41	13.41	16.90	6.31	6.21	6.10	6.10	5.88			
323.15	62.73	76.53	92.51	92.50	133.25	6.69	6.84	7.00	7.00	7.67	5.77	5.70	5.62	5.62	5.48			
333.15	67.20	81.64	98.45	98.44	141.77	5.44	5.38	5.34	5.34	5.30	5.12	5.04	4.97	4.97	4.83			
343.15	71.08	86.13	103.75	103.74	126.82	7.69	8.41	9.27	9.27	12.16	4.65	4.57	4.48	4.48	4.33			
353.15	76.15	91.97	110.58	110.57	159.61	13.12	15.06	17.36	17.36	23.47	3.72	3.64	3.58	3.58	3.48			
AARD	64.86	79.00	95.43	95.43	133.82	10.06	11.04	12.19	12.19	15.24	5.51	5.43	5.35	5.35	5.22			
PC-SAFT																		
Temperature [K]	k <sub>ij</sub> =0						k <sub>ij</sub> =1p						k <sub>ij</sub> =2p					
	NA	1A	2B	3B	4C	NA	1A	2B	3B	4C	NA	1A	2B	3B	4C			
303.15	17.80	10.36	5.32	5.33	15.06	8.12	7.77	8.31	8.31	10.22	7.34	6.30	5.36	5.36	3.47			
313.15	16.10	8.45	3.82	3.82	17.81	6.40	5.99	6.06	6.06	7.24	5.52	4.61	3.77	3.77	2.19			
323.15	14.26	6.38	3.57	3.57	20.69	5.07	4.58	4.15	4.15	4.14	4.65	3.88	3.30	3.30	2.13			
333.15	11.86	3.96	5.01	5.01	24.38	3.61	2.91	2.25	2.25	1.11	3.68	3.06	2.55	2.55	1.58			
343.15	9.30	2.27	8.11	8.11	28.23	3.52	3.15	3.03	3.03	3.50	2.91	2.28	1.79	1.79	0.92			
353.15	5.55	3.31	12.73	12.73	33.89	5.54	6.28	7.13	7.13	8.88	1.86	1.41	1.12	1.12	1.68			
AARD	12.48	5.79	6.43	6.43	23.34	5.36	5.11	5.15	5.15	5.85	4.33	3.59	3.00	3.00	2.00			

**Supplementary E5. Hydrogen sulfide (H<sub>2</sub>S) with ionic liquids results***Table S24. Deviations in pressure for H<sub>2</sub>S and [EMIM][TfO] using the RK-Aspen model.*

Temperature [K]	H <sub>2</sub> S		
	k <sub>ij</sub> =0	2p	4p
303.15	18.90	2.52	2.79
313.15	18.26	2.29	2.30
323.15	19.15	1.34	1.14

333.15	18.12	1.80	1.46
343.15	18.25	2.01	1.09
353.15	18.61	3.01	1.65
AARD	18.55	2.16	1.74

Table S25. Deviations in pressure for  $H_2S$  and  $[EMIM][TfO]$  using the CPA e PC-SAFT EoS.

Temperature [K]	CPA														
	k <sub>ij</sub> =0				1p				2p						
	NA	1A	2B	3B	4C	NA	1A	2B	3B	4C	NA	1A	2B	3B	4C
303.15	165.34	15.79	11.54	94.90	30.25	34.13	2.85	15.11	DU	21.90	43.79	3.86	13.30	DU	19.05
313.15	162.19	17.95	13.15	96.41	31.32	33.98	2.94	12.52	DU	18.15	38.15	3.80	11.80	DU	17.05
323.15	162.63	19.19	13.68	98.22	31.54	36.00	3.38	11.36	DU	16.03	34.71	2.90	11.57	DU	16.44
333.15	158.48	21.38	15.39	99.99	32.68	35.52	6.40	9.16	DU	12.92	29.40	3.49	9.82	DU	14.03
343.15	157.62	22.48	15.96	100.00	32.91	37.00	8.26	7.98	DU	11.12	25.90	3.26	9.08	DU	12.88
353.15	155.59	23.53	16.63	100.00	33.23	38.71	10.06	5.89	DU	8.48	21.74	3.95	7.33	DU	10.77
AARD	160.31	20.05	14.39	98.25	31.99	35.89	5.65	10.34	DU	14.77	32.28	3.54	10.48	DU	15.04
PC-SAFT															
Temperature [K]	k <sub>ij</sub> =0				1p				2p						
	N	1A	2B	3B	4C	NA	1A	2B	3B	4C	NA	1A	2B	3B	4C
	35.92	37.32	50.71	94.26	71.31	26.49	21.78	16.96	32.71	8.92	26.89	22.54	18.03	41.85	10.48
313.15	31.14	33.14	46.53	96.06	67.77	22.44	18.54	14.49	38.57	7.71	22.57	18.81	14.88	40.14	8.28
323.15	28.34	30.88	44.41	98.01	66.42	20.14	16.90	13.49	39.39	7.72	20.07	16.76	13.31	39.88	7.51
333.15	23.84	26.85	40.31	99.51	62.73	16.21	13.63	10.87	41.78	6.20	15.97	13.16	10.25	37.89	5.51
343.15	21.21	24.66	38.21	99.70	61.24	13.73	11.69	9.47	46.41	5.78	13.35	11.01	8.61	37.81	4.49
353.15	18.47	22.33	35.92	99.68	59.49	10.53	8.98	7.65	38.57	5.78	10.16	8.19	6.14	27.26	3.09
AARD	26.49	29.20	42.68	97.87	64.83	18.26	15.25	12.16	39.57	7.02	18.17	15.08	11.87	37.47	6.56

\* DU: Data Unavailable

Table S26. Deviations in pressure for  $H_2S$  and  $[OMIM][NTf_2]$  using the RK-Aspen model.

Temperature [K]	H <sub>2</sub> S			
	k <sub>ij</sub> =0	2p	4p	
303.15	38.43	14.98	4.95	
313.15	48.52	9.45	4.33	
323.15	53.39	4.84	3.78	
333.15	58.17	4.07	3.57	
343.15	70.74	8.93	2.17	
353.15	75.83	14.93	2.24	
AARD	57.51	9.53	3.51	

Table S27. Deviations in pressure for  $H_2S$  and  $[OMIM][NTf_2]$  using the CPA e PC-SAFT EoS

Temperature [K]	CPA															
	k <sub>ij</sub> =0						1p						2p			
	NA	1A	2B	3B	4C	NA	1A	2B	3B	4C	NA	1A	2B	3B	4C	
303.15	154.93	14.24	2.09	74.02	22.92	24.37	14.08	5.39	DU	5.47	15.55	14.08	2.11	DU	2.90	
313.15	175.61	12.35	3.64	83.71	21.38	15.92	12.22	3.73	DU	4.15	13.75	12.22	1.98	DU	3.66	
323.15	179.48	11.88	4.15	86.58	19.83	12.35	11.76	2.44	DU	3.51	12.21	11.76	1.74	DU	3.37	
333.15	182.87	11.05	5.12	89.20	18.24	11.63	10.93	1.80	DU	3.50	11.23	10.93	2.12	DU	3.55	
343.15	203.60	9.16	8.62	96.82	14.05	13.50	8.99	3.23	DU	4.01	9.40	8.99	1.40	DU	3.49	
353.15	205.63	9.01	10.39	98.26	11.65	18.12	8.85	4.96	DU	4.79	8.50	8.85	1.51	DU	3.17	
AARD	183.69	11.28	5.67	88.10	18.01	15.98	11.14	3.59	DU	4.24	11.77	11.14	1.81	DU	3.36	
PC-SAFT																
Temperature [K]	k <sub>ij</sub> =0						1p									
	NA	1A	2B	3B	4C	NA	1A	2B	3B	4C	NA	1A	2B	3B	4C	
	9.38	8.35	5.61	79.32	8.54	10.52	10.53	DU	10.11	9.08	7.52	5.92	DU	3.57		
313.15	6.83	5.38	6.10	87.48	12.53	7.03	6.76	6.81	DU	6.63	7.34	5.97	4.71	DU	3.07	
323.15	5.68	4.46	6.62	89.62	15.44	5.56	4.65	4.43	DU	3.74	5.78	4.43	3.33	DU	2.74	
333.15	5.08	4.48	8.23	91.62	18.61	4.87	3.67	2.97	DU	2.71	4.75	3.77	3.25	DU	2.88	
343.15	5.82	6.58	13.50	97.70	25.47	5.16	4.77	4.67	DU	5.33	3.70	2.76	1.85	DU	1.70	
353.15	7.92	9.34	17.17	98.71	29.89	6.98	7.13	7.80	DU	9.60	2.98	2.39	1.82	DU	2.15	
AARD	6.78	6.43	9.54	90.74	18.41	6.69	6.25	6.20	DU	6.35	5.60	4.47	3.48	DU	2.68	

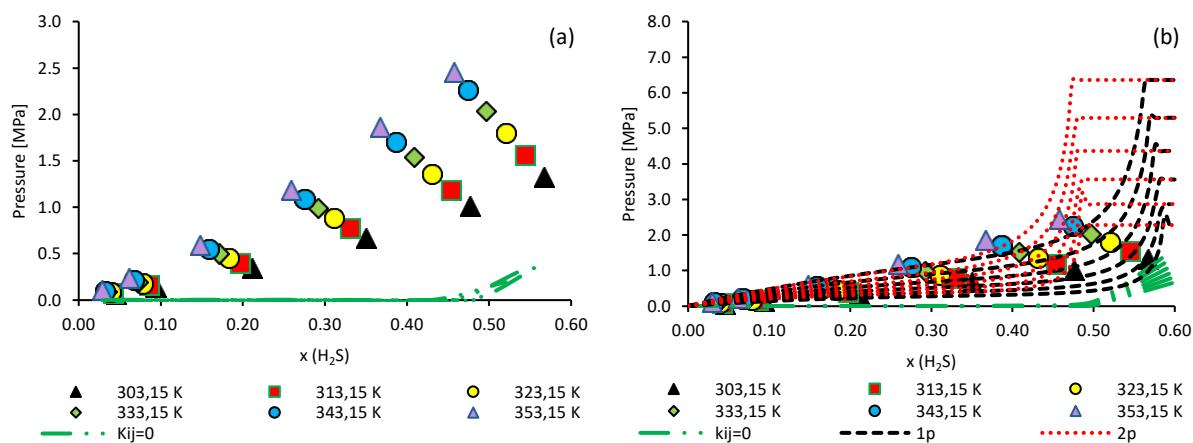


Figure S15.  $P\text{-}x$  results for  $\text{H}_2\text{S}$  and  $[\text{EMIM}][\text{TfO}]$ : (a) CPA EoS with  $k_{ij}=0$  for 3B associative scheme; (b) PC-SAFT EoS with  $k_{ij}=0$ , 1p e 2p for 3B associative scheme. Experimental data from Nematpour *et al.* [12].

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